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Synthesis of Coupling Matrix for Diplexers Based on a Self-adaptive Differential Evolution Algorithm

Bo Liu, *Senior Member, IEEE*, Hao Yang, Michael Lancaster, *Senior Member, IEEE*

Abstract—Diplexer coupling matrix synthesis often involves both analytical methods and optimization techniques. At present, general purpose optimization algorithms are used, but they need strong supporting information (e.g., high-quality starting points, very narrow search ranges) from analytical methods, which is not available or too complex to be obtained in many cases. Aiming to obtain the desired coupling matrix with highly reduced supporting information to relieve the pressure of analytical methods, a new optimization algorithm, called self-adaptive differential evolution for coupling matrix synthesis (SADEC), is proposed. Considering the landscape characteristics of diplexer coupling matrix synthesis problems, a new self-adaptive multi-population search framework and a self-adaptive algorithm parameter control strategy are proposed and organized in a particular way. The performance of SADEC is demonstrated by two all resonator-based narrow-band diplexers using large search ranges only with the requirement of matching the diplexer topology and no ad-hoc analysis is included. Experiments and comparisons show the high performance of SADEC and clear advantages compared to state-of-the-art global optimization methods. SADEC is also applicable to filter coupling matrix synthesis and is downloadable.

Index Terms—Coupling matrix, Coupling matrix synthesis, Diplexer, Differential evolution

I. INTRODUCTION

The coupling matrix model is often employed in modern filter and diplexer design [1]. Because of the direct connection between the coupling matrix and the geometric parameters of the physical design, the coupling matrix is a widely used tool to obtain the initial geometric design parameters before 3D full-wave electromagnetic (EM) simulation-based design optimization. References [2] and [3] show that both local optimization and global optimization-based EM simulation-driven design optimization methods can benefit from a good initial design for complex filters and diplexers. Therefore, high-quality synthesis of a coupling matrix is essential.

Coupling matrix synthesis methods can be mainly classified into three categories: analytical methods [4], [5], [6], optimization-based methods [7], [8], [9] and hybrid analytical and optimization methods [10], [11]. In analytical methods, the appropriate coupling coefficient and external quality factor values are analytically calculated based on the properties of the microwave device. They are theoretically sound and with guaranteed good results. Optimization-based methods, on the

other hand, obtain the appropriate coupling matrix through a black-box optimization process. Except for the selection of cost functions [12], [13], [9], much less theoretical analysis is involved, providing the advantages of ease of use and being general.

However, as the complexity of the response and topology increases, especially for multiport devices, both kinds of methods face challenges: analytical methods can become intricate and sometimes impossible to realize [14], optimization methods may have a low success rate even with fine tuning of the cost function and the search range [9], [15]. Traditional genetic algorithms or genetic algorithm-based memetic/hybrid algorithms and state-of-the-art global optimization algorithms (e.g., differential evolution (DE) [16], particle swarm optimization (PSO) [17]) are tested in our pilot experiments. The success rate is low for various diplexer coupling matrix synthesis problems.

Therefore, hybrid analytical and optimization-based methods are attracting much attention. In such methods, an optimization engine is employed, but the optimization problem is highly simplified based on analytical methods, such as a high-quality starting point [11], a well-organized synthesis process [10] or highly reduced search ranges [18]. Due to such strong supporting information, the optimization algorithm does not need to be strong. At present, the widely used methods are general purpose optimization methods, such as Nelder-Mead simplex method [19], sequential quadratic programming [20] and evolutionary algorithms (EAs), which are widely used in microwave engineering [21], [22], [23], [24].

However, the main application area of hybrid analytical and optimization-based methods is filter synthesis. To the best of our knowledge, for more complex topologies, such as the all resonator-based diplexer, which is a new and promising component in satellite communication systems, there are few matured coupling matrix synthesis methods. When applying the above hybrid method for diplexer synthesis, it is not easy to obtain a good enough starting point or the search range is not narrow enough in many cases, causing optimization not to be successful [15]. Hence, developing a strong optimization mechanism for complex coupling matrix synthesis, which can considerably relieve the pressure of the prior analytical analysis, is important to complement the state of the art for coupling matrix synthesis for multiport devices.

Aiming to fill this gap, an optimization method for coupling matrix synthesis for diplexers, called self-adaptive differential evolution for coupling matrix synthesis (SADEC), is proposed. The main innovations include a new self-adaptive multi-population search framework and a self-adaptive differential

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evolution algorithm parameter control strategy. Both of them are designed to tackle the landscape characteristics of the targeted problem. SADEC aims to:

- Obtain highly optimal solutions for diplexer coupling matrix synthesis with a high success rate;
- Do not rely on good initial values, highly reduced search ranges or other specific properties of the targeted design cases.

We believe that if these two goals are met, diplexer coupling matrix synthesis with weak, easy to obtain or highly reduced supporting information from analytical methods is expected to be successful in most cases. General purpose optimization techniques (e.g., sequential quadratic programming, PSO), which show difficulty for the targeted problem, can therefore be replaced.

The remainder of the paper is organized as follows. Section II introduces the basic techniques, including a brief introduction of the coupling matrix method and the standard differential evolution (DE) algorithm. Section III introduces the SADEC algorithm, including its main ideas, design of the new algorithm framework and algorithmic components and parameter setting. Section IV demonstrates SADEC by two all resonator-based diplexers. Large search ranges only with the requirement of matching the diplexer topology are used. Comparisons with standard DE and PSO are also provided. The concluding remarks are provided in Section V.

II. BASIC TECHNIQUES

A. The Coupling Matrix Method for Diplexer Design

The S-parameter design specifications of a diplexer can be calculated using the scaled external quality factors q_{ei} and the general matrix $[A]$ using the following equations [18]:

$$\begin{aligned} S_{11} &= \pm(1 - \frac{2}{q_{e1}}[A]_{1,1}^{-1}) \\ S_{i1} &= 2\frac{1}{\sqrt{q_{e1}q_{ei}}}[A]_{i,1}^{-1}, i = 2, \dots, n \end{aligned} \quad (1)$$

where n is the number of ports. The general matrix $[A]$ can be expressed as:

$$[A] = [q] + p[U] - j[m] \quad (2)$$

where $[q]$ is an $n \times n$ matrix with all entries zero, except for $q_{ii} = \frac{1}{q_{ei}}, i = 1, 2, \dots, n$ (i stands for the index of a resonator connected to an external port), $[U]$ is an $n \times n$ identity matrix, p is the complex lowpass frequency variable and $[m]$ is the general normalized coupling matrix, which is what SADEC targets at.

B. The Differential Evolution Algorithm

The DE algorithm [16] is the fundamentals of SADEC. DE is a population-based global optimization algorithm, which outperforms many EAs for continuous optimization problems [16] and is widely used in the EM design optimization domain. Nevertheless, DE is not the only choice, and other popular EAs (e.g., PSO, Evolution Strategy) may also be improved following similar ideas in this paper.

DE is an iterative method. In each iteration, the mutation operator is firstly applied to generate a population of mutant

vectors. A crossover operator is then applied to the mutant vectors to generate a new population. Finally, selection takes place and the corresponding candidate solutions from the old population and the new population compete to comprise the population for the next iteration.

In the t^{th} iteration, the i^{th} candidate solution in the population, P , can be represented as:

$$x^i(t) = [x_1^i, x_2^i, \dots, x_d^i] \quad (3)$$

where d is the number of design variables.

In DE, mutation is the main approach to explore the design space. There are a few different DE mutation strategies trading off the convergence speed and the population diversity in different manners. Arguably, the most widely used one is DE/rand/1 [16], which is as follows:

$$v^i(t+1) = x^{r1}(t) + F \cdot (x^{r2}(t) - x^{r3}(t)) \quad (4)$$

where x^{r1} , x^{r2} and x^{r3} are three different solutions randomly selected from the current population, P . v^i is the i^{th} mutant vector in the population after mutation. $F \in (0, 2]$ is a control parameter, called the scaling factor.

Crossover is then applied to the population of mutant vectors to produce the child population U , which works as follows:

- 1 Randomly select a variable index $j_{rand} \in \{1, \dots, d\}$,
- 2 For each $j = 1$ to d , generate a uniformly distributed random number $rand$ from $(0, 1)$ and set:

$$u_j^i(t+1) = \begin{cases} v_j^i(t+1), & \text{if } (rand \leq CR) | j = j_{rand} \\ x_j^i(t), & \text{otherwise} \end{cases} \quad (5)$$

where $CR \in [0, 1]$ is a constant called the crossover rate.

Following that, the selection operation decides on the population of the next iteration, which is often based on a one-to-one greedy selection between P and U . Considering a minimization problem, the selection operator is:

$$x^i(t+1) = \begin{cases} u^i(t+1), & \text{if } f(u^i(t+1)) < f(x^i(t)) \\ x^i(t), & \text{otherwise} \end{cases} \quad (6)$$

III. THE SADEC ALGORITHM

A. Challenges and Motivations

Aiming to propose a general method for diplexer coupling matrix synthesis, case-specific information is not included in the cost function. Our cost function only involves violation of S-parameter constraints, such as $\max\{\max(|S_{11}|) - (-20\text{dB}), 0\}$ for the constraint of $\max|S_{11}| < -20\text{dB}$ in the passband(s). The cost function is defined as the sum of normalized S-parameter constraint violations. For normalization, the violation of each constraint for each candidate solution is divided by the maximum constraint violation so far for the corresponding constraint. Examples are shown in Section IV. Transmission and reflection zeros are not used due to generality consideration. Transmission zeros do not always exist. We also found that for some complex synthesis problems, there are many solutions with very close transmission

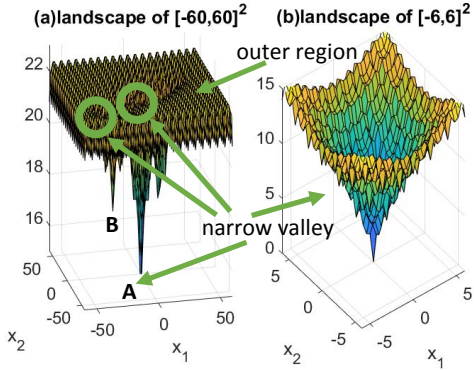


Fig. 1. An illustrative figure of diplexer coupling matrix synthesis problem landscape (The Ackley benchmark test function [25] is used for illustration)

and/or reflection zeros compared to the desired ones, but the S-parameter response is far away from the specifications.

Using the above cost function, by studying various diplexer coupling matrix synthesis problems (e.g., sampling and sweeping), Fig. 1 (illustrative figure) shows the characteristics of the landscape. It can be seen that: (1) If without an ad-hoc selection of the search range, the optimal regions locate in several narrow valleys of the search space and the outer region is flat. This characteristic is understandable because most diplexers are narrow band, and resonance only happens in very particular design parameters. (2) The optimal regions are separated because these narrow valleys are not connected with each other. (3) The best solution in most of the narrow valleys is only a local optimum (point B in Fig. 1), which is not useful (an example is shown in Section IV (A)). (4) Even in a narrow valley, the landscape is multimodal (has local optima).

EAs are stochastic optimization methods and there is always a balance between the exploration ability and the probability to find the correct search direction [26]. In a stochastic search process, if the diversity of possible movements is limited, it is easy to get trapped in a local optimum. When the diversity of possible movements increases, the capacity of exploring unknown space is promoted, but the probability to find the correct search direction decreases considerably. The characteristics of the targeted landscape require the optimization algorithm having a good exploration ability because it is multimodal. However, it also requires the algorithm having a high capacity to find the correct search direction because the optima locate in narrow valleys. In addition, most of the narrow valleys only provide local optima even if they are visited. Therefore, it is not a surprise that modern EAs, such as standard DE and PSO have a very low success rate. Our pilot experiments show that standard DE and PSO have difficulty in converging at the global optimum and may converge at a local optimum (i.e., point B in Fig. 1).

In the computational intelligence field, various improved DE and PSO are proposed [27] and many of them focus on jumping out of local optima. Their general idea is to promote the exploration ability. However, these methods do not seem suitable for the targeted problem. These methods

target at highly multimodal problems but their optimal regions are not narrow and not separated [25]. Hence, finding the correct search direction is not a main consideration for those methods, but it is an important challenge for the coupling matrix synthesis problem. Arguably, the benchmark test problem with the narrowest optimal region used in the computational intelligence field is the Ackley function [25], while our experiments show that the optimal region of the targeted problem is much narrower than that of the Ackley function. Therefore, promoting exploration ability makes the optimization algorithm be trapped in the outer region when synthesizing diplexer coupling matrix, which is verified by our pilot experiments. For example, several popular improved DE even cannot detect the narrow valleys.

To the best of our knowledge, there are few works focusing on identifying the correct search direction for the targeted landscape. Therefore, the goal of the SADEC algorithm is to increase the probability of finding and preserving the correct search direction while maintaining its exploration ability. SADEC is based on DE and the design of it is described in Section III (B) and (C).

B. The Self-adaptive Parameter Control Strategy

There are four key algorithmic parameters in DE, which are the population size (NP), the mutation strategy, the scaling factor (F) and the crossover rate (CR). The selection of them has a significant influence on the performance of DE for complex optimization problems [28], [29]. The mutation strategy and the scaling factor control the exploration of the decision space. In particular, the mutation strategy can be considered as the choice of the search direction, while the scaling factor can be considered as the step length. An example is the DE/rand/1 mutation (4). Selecting different kinds of mutation strategies and scaling factor leads to different capability of exploration. Besides, by increasing the size of the population, the exploration ability is promoted. As described above, the probability of finding the correct search direction is therefore decreased. According to (5), the crossover operator decides how many decision variables in expectation are changed in a population member. Thus, it decides to what extent that the visited search patterns (or search directions) can be changed/preserved.

A central question then becomes how to control these parameters so as to promote the probability of finding and preserving the correct search directions while maintaining the exploration ability. As described in Section III (A), there are almost no guidelines for the landscapes of the targeted problem. Hence, empirical tests using various coupling matrix synthesis problems with different complexity are carried out and the following observations are obtained: (1) The inventor of DE suggests that the population size NP should be around $5 \times D$ to $10 \times D$ [16]. Our experiments show that when using the DE/rand/1 mutation with a reasonable scaling factor, $NP = 5 \times D$ always provides enough exploration ability. (2) When using DE mutation strategies with higher exploration ability than DE/rand/1 (e.g., DE/rand/2 [16]), the probability of visiting the narrow valleys decreases. Given the settings of $NP = 5 \times D$ and the DE/rand/1 mutation, the control of F and CR is discussed in the following.

Considering the characteristics of the targeted landscape, large F is needed to explore the decision space so as to get access to the narrow valleys. Small F is also needed to perform local exploitation in the narrow valley. [16] suggests that F should not be smaller than 0.4, while a widely used parameter study [30] argues that the lower bound of F is problem dependent. Both studies suggest that if F is larger than 1.0, the convergence speed will decrease. [16] and [30] recommend to use $F = 0.5$ and $F = 0.6$ as a default value, respectively. Considering above, SADEC uses the following method to decide the scaling factor:

$$F_{temp} = norm(0.5, 0.25)$$

$$F^i(t) = \begin{cases} 1, & \text{if } F_{temp} > 1 \\ 0.1, & \text{if } F_{temp} < 0.1 \\ F_{temp}, & \text{otherwise} \end{cases} \quad (7)$$

where $norm(0.5, 0.25)$ is a Gaussian distributed random number with a mean of 0.5 and a standard deviation of 0.25.

It can be seen that: (1) Because of the Gaussian distribution, there is about 68% probability, the generated F is between 0.25 to 0.75 (near the recommended default values). For about 27% probability, F is between 0.1 to 0.25 or between 0.75 to 1 (emphasizes exploration or exploitation in particular). (2) For each candidate solution in each iteration, there is a separate F . In this way, different kinds of candidate designs have the opportunity to use various kinds of F (i.e., step size) in an appropriate range to either perform exploration or exploitation.

In terms of CR control strategy, various DE parameter studies show different recommendations [16], [30], [31]. Unfortunately, none of them works in our pilot tests using diplexer coupling matrix synthesis problems. In our empirical study, using various candidate solutions (x) and their mutant vectors (v) in the optimization process, a number of child candidates (u) are generated for a certain CR value. The number of successful crossovers, for which, u is better than x , can be observed. Two main observations include: (1) For different candidate solutions, there is not a universal workable CR value and the fitted CR values can be very different. (2) In many cases, the workable CR value for a candidate solution spans in a narrow range (e.g., 0.4-0.5). This explains why a fixed setting rule of CR cannot work for the targeted problem. Therefore, a possible way is to explore random CR values and inherit the workable ones, which is shown as follows:

$$CR_{temp} = 0.1 + rand_1 \times 0.8$$

$$CR^i(t) = \begin{cases} CR_{temp}, & \text{if } rand_2 < 0.1 \\ CR^i(t-1), & \text{otherwise} \end{cases} \quad (8)$$

where $rand$ is a uniformly distributed random number between 0 and 1. $CR(1) = 0.9$, which is based on the suggested default value in [16].

It can be seen that for 10% probability, CR can be any value between 0.1 and 0.9 (the possible range suggested by [16]); Otherwise, CR is inherited from the last iteration. Note that each candidate solution in the optimization process has its own CR value. Pilot experiments show that there is a considerable probability that a feasible CR for a certain candidate solution is sampled and inherited in the optimization process. Comparisons with several widely used self-adaptive

setting rules (e.g., [32]) show that this control method has the highest success rate.

C. The Self-adaptive Multi-population Search Framework

Despite employing the above self-adaptive parameter control mechanism, obtaining the appropriate F and CR values cannot be guaranteed. Sometimes, the optimization converges to narrow valleys that only contain local optima (such as point B in Fig. 1). In almost all of the local optima that we have encountered, some resonance happens in undesired frequency ranges, while the others are correct. Hence, a new operator, called self-adaptive return operator, is activated when the optimization is judged to be trapped in local optima, which can often be observed in earlier iterations if it happens. The judgment of being trapped in local optima is based on two conditions: (1) The maximum standard deviation of decision variables in the current population is smaller than a predefined threshold δ ; (2) The number of reflection zeros in any passband is incorrect. Using the return operator, the optimization returns to the original initial population, and the F and CR will be re-sampled based on (7) and (8) and the optimization process will restart. The effectiveness of this operator is shown by various test cases, and an example is shown in Section IV (B).

Reference [7] shows that the choice of initial population has an effect on the final result for coupling matrix synthesis problems. Our pilot experiments show a similar observation that some initial populations have a higher probability to obtain the desired global optimum than others using the same process in Section III (B). Hence, a multi-population framework is proposed to increase the success rate.

Two populations are used. For one of them (P), the initialization is based on random sampling. The initialization of the other one (\bar{P}) is the opposite population of P , which is composed by:

$$\bar{x}^i(1) = a + b - x^i(1) \quad (9)$$

where $x^i(1)$ is the i^{th} candidate solution in initial P , $\bar{x}^i(1)$ is the corresponding candidate solution in initial \bar{P} , $[a, b]^d$ is the search range. Experiments show that in many cases, if the optimization is not successful when using P as the initial population, using \bar{P} as the initial population has much larger success rate than using another randomly sampled population. This is understandable because \bar{P} is often the best complement of P , covering search patterns that do not exist in P as much as possible.

D. The General Framework of the SADEC Algorithm

The flow diagram of the SADEC algorithm is shown in Fig. 2, which consists the following steps.

- Step 1:** Initialize P and \bar{P} using the method in Section III (C). Initialize NP to be $5 \times D$. Initialize CR to be 0.9 for the crossover of the first iteration.
- Step 2:** Check if the stopping criteria (e.g., a certain number of iterations) are met. If yes, output the result; otherwise, go to Step 3.

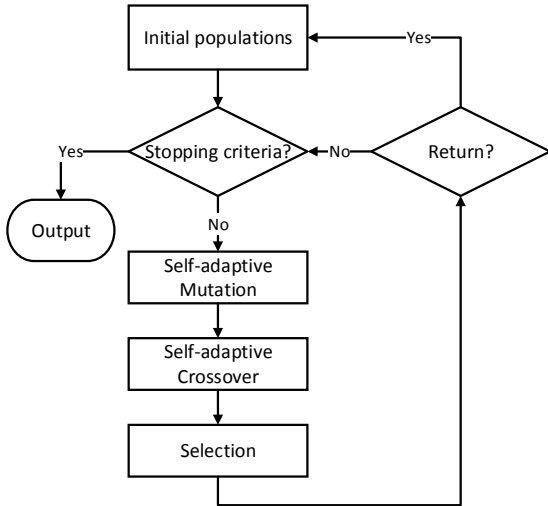


Fig. 2. The flow diagram of SADEC

- Step 3:** Apply the DE/rand/1 mutation (4) on P and \bar{P} to generate mutant vectors V_p and $V_{\bar{p}}$. Use (7) to generate F values for the composing of each mutant vector.
- Step 4:** Apply the crossover operator (5) on V_p and $V_{\bar{p}}$ to generate U_p and $U_{\bar{p}}$. If it is in the first iteration, $CR = 0.9$; otherwise, use (8) to generate CR for each crossover.
- Step 5:** Apply the selection operator (6) to generate P and \bar{P} for the next iteration.
- Step 6:** Check if the return criteria for P or \bar{P} are met. If yes, return to the corresponding initial population(s) and go to Step 2; otherwise, go to Step 3.

The only user defined algorithmic parameter in SADEC is δ when judging whether the population is trapped in a local optimum or not, which is the threshold of the maximum standard deviation of the decision variables in the current population. This threshold should be small enough making sure that the difference between the members of the current population is small, indicating that convergence happens. Clearly, this parameter is not sensitive if it is small enough, and the worst case is wasting function evaluations when the search sticks in a narrow valley that only contains a local optimum. Considering the search range of (normalized) coupling matrix optimization problems, which is often around $[-1, 1]$, a recommended setting is $\delta = 0.01$.

IV. NUMERICAL RESULTS AND COMPARISONS

SADEC has been tested by coupling matrix synthesis problems of 7 real-world all resonator-based diplexers. SADEC obtains high-quality results with very high success rate to all of them. In this section, two examples are used to demonstrate different operators in SADEC. To the best of our knowledge, there are no general global optimization-based methods to solve them. The two diplexers have Chebyshev response, but SADEC is applicable to any response (e.g., Butterworth response) that can be generated by a coupling matrix. In both

examples, the sum of normalized constraint violations is set as the cost function to be minimized. Because we are working with normalized values, practical diplexers can in principle be made at any frequency with any type of resonator [1]. Hence, we only concentrate on the normalized coupling matrix in the following.

For both examples, 20 runs are carried out for SADEC, standard DE and PSO and the results are compared statistically. DE and PSO are state-of-the-art global optimization methods, which have both strong global exploration and local exploitation ability. The stopping criterion for SADEC is that the maximum number of activating the return operator is 3 and the maximum number of iterations after each activation (if there is) is 1000. If the return operator is not activated, the maximum number of iterations is 1000. The stopping criterion for DE and PSO is also 1000 iterations. In all the runs for the three methods, the convergence happens before 1000, either stuck in a local optimum, or obtains a successful result.

For the parameter setting of standard DE, the population size is the same as SADEC, the same DE/rand/1 mutation is used. As suggested by [16], [33], $F = 0.5$, $CR = 0.9$ are used. PSO is implemented using the MATLAB Global Optimization Toolbox. The star topology is used. As suggested by [34], the cognitive coefficient and the social coefficient are both set to 2. According to [35], when the swarm size is larger than 50, PSO is not sensitive to the size of the population. Similar to DE, to improve the probability of finding the correct search direction, larger swarm size should not be used. Hence, the swarm size is set to 50. There are various methods to set the inertia weight. Our experiments show that using a constant inertia weight of 0.4 shows the best performance, which is used for comparison.

The examples are run on a PC with Intel 3.5 GHz Core (TM) i7 CPU and 8 GB RAM under Windows operating system. Since each function evaluation costs around 1 second, computational time is not a problem. Each SADEC run often costs about 40 minutes to 1 hour, while each DE and PSO run often costs about 20 minutes. In the SADEC optimization, the number of cost function calls for example 1 is around 1660 and that for example 2 is around 2870. In each cost function evaluation, 4000 frequencies are swept.

A. Example 1

The first example is a 10 resonator diplexer with a symmetrical Chebyshev response [36] (Fig. 3), which is a moderate test case among all the problems. This is a novel all-resonator-based diplexer topology that eliminates the need of additional common junction such as T-junction or power splitter. It is especially suitable for applications that need reduced size and volume of the circuit. A full description is in [36]. Due to the symmetry of the response and topology, the total number of variables in the coupling matrix is reduced to 9 [36]. The external quality factors can be straightforwardly calculated, which are $qe_1 = 1.943$, $qe_2 = qe_3 = 3.886$. The ranges of the design variables are in Table I. The design variables are the coupling matrix elements m_{ij} defined in (2). It can be seen that the search range is decided without any careful

Table I: Ranges of the 9 decision variables for example 1

Variables	m_{12}	m_{23}	m_{34}	m_{45}	m_{56}
Lower bound	0	0	0	0	0
Upper bound	1	1	1	1	1
Variables	m_{33}	m_{44}	m_{55}	m_{66}	
Lower bound	0	0	0	0	
Upper bound	1	1	1	1	

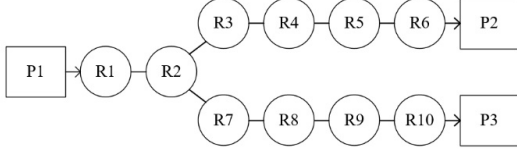


Fig. 3. The Topology of Example 1

selection and no additional information is provided to SADEC. The design specifications over the normalized frequency are: two passbands (PB_1 and PB_2) are with same bandwidth of 0.5 centered at -0.75 and 0.75 and the $\max(|S_{11}|)$ within the passband should be at least less than -20 dB. The normalized stopbands for channel 1 (PB_{1L} and PB_{1R}) are from -2 to 0.25 and from 1.25 to 2 , where the $\max(|S_{21}|)$ should be less than -20 dB. The normalized stopbands for channel 2 (PB_{2L} and PB_{2R}) are from -2 to -1.25 and from -0.25 to 2 , where the $\max(|S_{31}|)$ should be less than -20 dB. The design specifications are:

$$\begin{aligned}
 PB_1 &\leq -20 \text{ dB} \\
 PB_2 &\leq -20 \text{ dB} \\
 PB_{1L} &\leq -20 \text{ dB} \\
 PB_{1R} &\leq -20 \text{ dB} \\
 PB_{2L} &\leq -20 \text{ dB} \\
 PB_{2R} &\leq -20 \text{ dB}
 \end{aligned} \tag{10}$$

where

$$\begin{aligned}
 PB_1 &= \max(|S_{11}|), 0.5 \text{ to } 1 \\
 PB_2 &= \max(|S_{11}|), -1 \text{ to } -0.5 \\
 PB_{1L} &= \max(|S_{21}|), -2 \text{ to } 0.25 \\
 PB_{1R} &= \max(|S_{21}|), 1.25 \text{ to } 2 \\
 PB_{2L} &= \max(|S_{31}|), -2 \text{ to } -0.75 \\
 PB_{2R} &= \max(|S_{31}|), -0.25 \text{ to } 2
 \end{aligned} \tag{11}$$

where the numbers in (11) are normalized frequencies.

The cost function is defined as:

$$\begin{aligned}
 f_1 &= \frac{\max(PB_1 - (-20), 0)}{M_{PB_1}} + \frac{\max(PB_2 - (-20), 0)}{M_{PB_2}} \\
 &+ \frac{\max(PB_{1L} - (-20), 0)}{M_{PB_{1L}}} + \frac{\max(PB_{1R} - (-20), 0)}{M_{PB_{1R}}} \\
 &+ \frac{\max(PB_{2L} - (-20), 0)}{M_{PB_{2L}}} + \frac{\max(PB_{2R} - (-20), 0)}{M_{PB_{2R}}}
 \end{aligned} \tag{12}$$

where M_{PB_1} is the $\max\{\max(PB_1 - (-20), 0)\}$ so far (i.e., the maximum violation of the $PB_1 \leq -20$ dB constraint, found so far), so do the others.

A typical response of SADEC is shown in Fig. 4 and the corresponding optimal design variables are shown in Table II. Other normalized coupling coefficients are: $m_{27} = m_{23}$, $m_{78} = m_{34}$, $m_{89} = m_{45}$, $m_{9,10} = m_{56}$, $m_{77} = -m_{33}$, $m_{88} = -m_{44}$, $m_{99} = -m_{55}$, $m_{10,10} = -m_{66}$. Plugging in the optimal

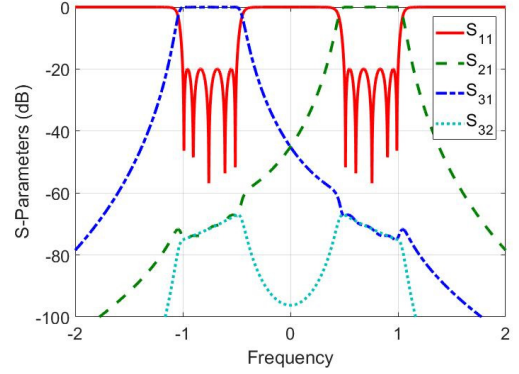


Fig. 4. Example 1: Response of a typical optimized solution by SADEC

Table II: A typical optimal result for example 1

Variables	m_{12}	m_{23}	m_{34}	m_{45}	m_{56}
Values	0.8204	0.2856	0.1625	0.1598	0.2170
Variables	m_{33}	m_{44}	m_{55}	m_{66}	
Values	0.7004	0.7442	0.7478	0.7487	

values to (2) and then to (1), the response can be obtained. The average optimized responses of SADEC, standard DE and PSO are shown in Table III. It can be seen that SADEC obtains successful results and is much better than DE and PSO in terms of optimization quality for this example.

The most important criterion for comparison is the success rate. In a diplexer design flow, the coupling matrix synthesis provides an initial design for 3D EM simulation-driven design optimization, rather than the final design. Hence, we define a successful result based on the following rules: (1) The reflection zeros are located in proper frequency ranges and the number is correct. A poor example is shown in Fig. 5. We consider that it is a local optimum, because performing various kinds of local optimization (e.g., sequential quadratic programming) from this starting point cannot find a better solution. When it comes to 3D EM simulation-driven local optimization, experiments show that using such a starting point often cannot obtain a successful final design. (2) The S-parameter design specifications are (almost) satisfied.

Using the above rules, the success rate of SADEC is 20/20, while those for DE and PSO are 4/20 and 1/20, respectively. Most DE and PSO runs obtain solutions like Fig. 5 (like point B in Fig. 1). For SADEC, in 17/20 runs, the return operator is not activated to either P or \bar{P} , which means that successful results are obtained directly using the self-adaptive parameter control strategy starting from both P and \bar{P} . In the other 3 runs, the return operator is only activated for once and

Table III: Optimized results using different methods for example 1 (average of 20 runs, in dB)

Methods	PB_1	PB_2	PB_{1L}	PB_{1R}	PB_{2L}	PB_{2R}
SADEC	-19.92	-19.92	-27.64	-23.15	-23.36	-27.40
DE	-14.97	-14.97	-27.23	-20.22	-23.36	-27.40
PSO	-5.29	-5.25	-20.00	-19.97	-19.98	-20.00

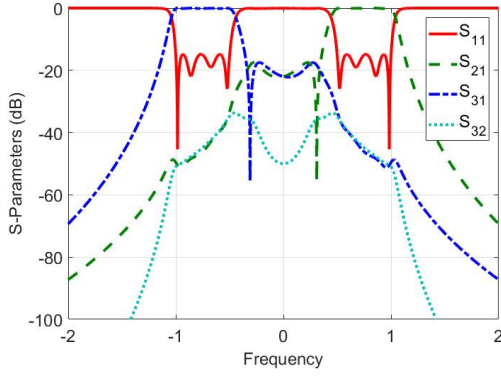


Fig. 5. A local optimum (example 1)

successful results are obtained. This verifies the considerable improvement of the capacity of finding and preserving correct search directions compared to standard DE, thanks to the algorithm parameter control strategy in Section III (B).

B. Example 2

The second example is a 12 resonator diplexer with a cross-coupling topology shown in [18] (Fig. 6). This topology allows the design of diplexers with sharp rejection in the guard band and is especially suitable for applications that require a reduced guard bandwidth. A full description is in [18]. A cross coupling between resonators 2 and 5 is introduced in a quadruplet to provide a pair of transmission zeros for both channels. By using the symmetry characteristics of the diplexer, the total number of variables is reduced to 12 [18]. The ranges of design variables are in Table IV. Again, the search range is decided without any careful selection and no additional information is provided to SADEC. The design specifications over the normalized frequency are: two passbands (PB_1 and PB_2) are with same bandwidth of 0.5 centered at -0.75 and 0.75 and the $\max(|S_{11}|)$ within the passband should be at least less than -20 dB. The constraints for the middle guard bands (PB_{1M} and PB_{2M}) (-0.3 to 0.3) of channel 1 and 2 are that $\max(|S_{21}|)$ and $\max(|S_{31}|)$ should be less than -40 dB due to the introduction of transmission zeros. The $\max(|S_{21}|)$ for the right stopband of channel 1 (PB_{1R}) (1.2 to 2) and $\max(|S_{31}|)$ for the left stopband of channel 2 (PB_{2L}) (-2 to -1.2) should be less than -20 dB. Therefore, the optimization problem is formulated as:

$$\begin{aligned}
 PB_1 &\leq -20 \text{ dB} \\
 PB_2 &\leq -20 \text{ dB} \\
 PB_{1M} &\leq -40 \text{ dB} \\
 PB_{2M} &\leq -40 \text{ dB} \\
 PB_{1R} &\leq -20 \text{ dB} \\
 PB_{2L} &\leq -20 \text{ dB}
 \end{aligned} \tag{13}$$

where

$$\begin{aligned}
 PB_1 &= \max(|S_{11}|), 0.5 \text{ to } 1 \\
 PB_2 &= \max(|S_{11}|), -1 \text{ to } -0.5 \\
 PB_{1M} &= \max(|S_{21}|), -0.3 \text{ to } 0.3 \\
 PB_{2M} &= \max(|S_{31}|), -0.3 \text{ to } 0.3 \\
 PB_{1R} &= \max(|S_{21}|), 1.2 \text{ to } 2 \\
 PB_{2L} &= \max(|S_{31}|), -2 \text{ to } -1.2
 \end{aligned} \tag{14}$$

Table IV: Ranges of the 12 decision variables for example 2

Variables	m_{12}	m_{23}	m_{34}	m_{45}	m_{56}	m_{67}
Lower bound	0	0	0	0	0	0
Upper bound	1	1	1	1	1	1
Variables	m_{78}	m_{89}	m_{77}	m_{88}	m_{99}	m_{25}
Lower bound	0	0	0	0	0	0
Upper bound	1	1	1	1	1	1

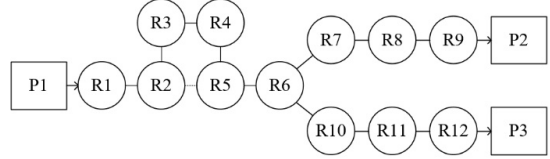


Fig. 6. The Topology of Example 2

where the numbers in (14) are normalized frequencies.

The cost function is defined as:

$$\begin{aligned}
 f_2 &= \frac{\max(PB_1 - (-20), 0)}{M_{PB_1}} + \frac{\max(PB_2 - (-20), 0)}{M_{PB_2}} \\
 &+ \frac{\max(PB_{1M} - (-40), 0)}{M_{PB_{1M}}} + \frac{\max(PB_{2M} - (-40), 0)}{M_{PB_{2M}}} \\
 &+ \frac{\max(PB_{1R} - (-20), 0)}{M_{PB_{1R}}} + \frac{\max(PB_{2L} - (-20), 0)}{M_{PB_{2L}}}
 \end{aligned} \tag{15}$$

where M_{PB_1} is the $\max\{\max(PB_1 - (-20), 0)\}$ so far (i.e., the maximum violation of the $PB_1 \leq -20$ dB constraint, found so far), so do the others.

A typical response of SADEC is shown in Fig. 7 and the corresponding optimal design variables are shown in Table V. Other normalized coupling coefficients are: $m_{6,10} = m_{67}$, $m_{10,11} = m_{78}$, $m_{11,12} = m_{89}$, $m_{10,10} = -m_{77}$, $m_{11,11} = -m_{88}$, $m_{12,12} = -m_{99}$. The average optimized responses of SADEC, standard DE and PSO are shown in Table VI. It can be seen that SADEC obtains successful results and is much better than DE and PSO in terms of optimization quality for

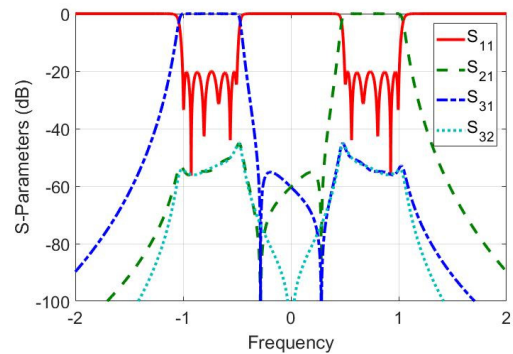


Fig. 7. Example 2: Response of a typical optimized solution by SADEC

Table V: A typical optimal result for example 2

Variables	m_{12}	m_{23}	m_{34}	m_{45}	m_{56}	m_{67}
Values	0.8278	0.3519	0.5786	0.2450	0.7609	0.2087
Variables	m_{78}	m_{89}	m_{77}	m_{88}	m_{99}	m_{25}
Values	0.1558	0.2142	0.7395	0.7495	0.7501	0.1955

Table VI: Optimized results using different methods for example 2 (average of 20 runs, in dB)

Methods	PB_1	PB_2	PB_{1M}	PB_{2M}	PB_{1R}	PB_{2L}
SADEC	-19.82	-19.83	-32.88	-46.92	-47.14	-32.61
DE	-9.05	-9.05	-26.41	-38.41	-38.39	-26.23
PSO	-3.19	-3.17	-19.94	-39.69	-39.71	-19.92

this example.

In this example, the success rate of SADEC is 20/20, while those for DE and PSO are 0/20 and 0/20, respectively. In 11/20 runs, the return operator is not activated to either P or \bar{P} in SADEC. Among these 11 runs, successful results are obtained from either P or \bar{P} in 10 of them (only starting from P or \bar{P} obtains successful results); for the other 1 run, successful results are obtained from both P and \bar{P} . This verifies that using two opposite populations, P and \bar{P} , in initialization establishes an effective complementation. Among the other 9 runs, the return operator is only activated for once in 7 of them; among 2/9 runs, the return operator is activated for twice and successful results are obtained. These 9 runs verify the effectiveness of the return operator to avoid converging into a narrow valley that only contains local optima.

It is intuitive that with the increase of the number of decision variables, the valley that contains the global optimum is narrower and narrower with respect to the decision space. This causes any optimization algorithm, including SADEC, to have difficulty in detecting the narrow valley. We found that for coupling matrix synthesis problems with more than 25 design variables, the success rate of SADEC is low if using large search ranges only with the requirement of matching the topology (e.g., $[-1, 1]^{25}$). In such cases, the support from analytical methods which reasonably narrow down the search ranges is needed. Note that SADEC does not aim to replace the analytical methods; instead, it aims to provide a much stronger optimizer than existing general purpose optimizers applied in hybrid analytical and optimization-based coupling matrix synthesis methods.

V. CONCLUSION

In this paper, the SADEC algorithm for diplexer coupling matrix synthesis has been proposed. SADEC aims at filling the gap that strong supporting information (e.g., high-quality starting points, narrow enough search ranges) from analytical methods is essential for the success of diplexer coupling matrix synthesis when employing available general purpose optimizers. SADEC focuses on proposing a stronger optimization mechanism specially for the targeted problem, which only requires weak, easy to obtain or highly reduced supporting information in most cases. Experiments show that SADEC is able to obtain highly optimized coupling matrix solutions with very high success rate even without ad-hoc supporting information for various diplexers. Much better solution quality and success rate are shown compared to state-of-the-art global optimization methods, DE and PSO. These results are achieved by our self-adaptive parameter control strategy and self-adaptive multi-population search framework.

Future works include developing software tools using SADEC and coupling matrix synthesis for multiplexers.

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REFERENCES

- [1] J.-S. G. Hong and M. J. Lancaster, *Microstrip filters for RF/microwave applications*. John Wiley & Sons, 2004, vol. 167.
- [2] J. W. Bandler, R. M. Biernacki, S. H. Chen, P. A. Grobelyny, and R. H. Hemmers, "Space mapping technique for electromagnetic optimization," *IEEE Trans. Microw. Theory Techn.*, vol. 42, no. 12, pp. 2536–2544, Dec 1994.
- [3] B. Liu, H. Yang, and M. J. Lancaster, "Global optimization of microwave filters based on a surrogate model-assisted evolutionary algorithm," *IEEE Trans. Microw. Theory Techn.*, vol. 65, no. 6, pp. 1976–1985, Jun 2017.
- [4] A. Atia, A. Williams, and R. Newcomb, "Narrow-band multiple-coupled cavity synthesis," *IEEE Trans. Circuits Syst.*, vol. 21, no. 5, pp. 649–655, May 1974.
- [5] R. J. Cameron, "General coupling matrix synthesis methods for chebyshev filtering functions," *IEEE Trans. Microw. Theory Techn.*, vol. 47, no. 4, pp. 433–442, Apr 1999.
- [6] S. Tamiazzo and G. Macchiarella, "Synthesis of cross-coupled filters with frequency-dependent couplings," *IEEE Trans. Microw. Theory Techn.*, vol. 65, no. 3, pp. 775–782, Mar 2017.
- [7] M. Uhm, S. Nam, and J. Kim, "Synthesis of resonator filters with arbitrary topology using hybrid method," *IEEE Trans. Microw. Theory Techn.*, vol. 55, no. 10, pp. 2157–2167, Oct 2007.
- [8] G. Nicholson and M. Lancaster, "Coupling matrix synthesis of cross-coupled microwave filters using a hybrid optimisation algorithm," *IET Microw., Antennas Propag.*, vol. 3, no. 6, pp. 950–958, Sep 2009.
- [9] X. Shang, Y. Wang, G. Nicholson, and M. J. Lancaster, "Design of multiple-passband filters using coupling matrix optimisation," *IET Microw., Antennas Propag.*, vol. 6, no. 1, pp. 24–30, Jan 2012.
- [10] L. Szydlowski, A. Lamecki, and M. Mrozowski, "A novel coupling matrix synthesis technique for generalised chebyshev filters with resonant source–load connection," *IEEE Trans. Microw. Theory Techn.*, vol. 61, no. 10, pp. 3568–3577, Oct 2013.
- [11] D. Tubail and T. Skaik, "Synthesis of coupled resonator-based multiplexers with generalised structures using coupling matrix optimisation," *Elect. Lett.*, vol. 51, no. 23, pp. 1891–1893, Nov 2015.
- [12] M. Mokhtari, J. Bornemann, K. Rambabu, and S. Amari, "Coupling-matrix design of dual and triple passband filters," *IEEE Trans. Microw. Theory Techn.*, vol. 54, no. 11, pp. 3940–3946, Nov 2006.
- [13] A. Lamecki, P. Kozakowski, and M. Mrozowski, "Fast synthesis of coupled-resonator filters," *IEEE Microw. Wirel. Compon. Lett.*, vol. 14, no. 4, pp. 174–176, Apr 2004.
- [14] W. A. Atia, K. A. Zaki, and A. E. Atia, "Synthesis of general topology multiple coupled resonator filters by optimization," in *Intel Microw. Symp. Digest*, vol. 2. IEEE, 1998, pp. 821–824.
- [15] W. Xia, "Diplexers and multiplexers design by using coupling matrix optimisation," Ph.D. dissertation, University of Birmingham, 2015.
- [16] K. Price, R. Storn, and J. Lampinen, *Differential evolution: a practical approach to global optimization*. Springer-Verlag New York Inc, 2005.
- [17] J. Kennedy, "Particle swarm optimization," in *Encyc. Mach. Learn.* Springer, 2011, pp. 760–766.
- [18] X. Shang, Y. Wang, W. Xia, and M. J. Lancaster, "Novel multiplexer topologies based on all-resonator structures," *IEEE Trans. Microw. Theory Techn.*, vol. 61, no. 11, pp. 3838–3845, Nov 2013.
- [19] J. C. Lagarias, J. A. Reeds, M. H. Wright, and P. E. Wright, "Convergence properties of the nelder–mead simplex method in low dimensions," *SIAM Journal Optim.*, vol. 9, no. 1, pp. 112–147, Mar 1998.
- [20] P. T. Boggs and J. W. Tolle, "Sequential quadratic programming," *Acta numerica*, vol. 4, no. 1, pp. 1–51, Jan 1995.
- [21] Ł. Januszkiwicz, P. Di Barba, and S. Hausman, "Field-based optimal placement of antennas for body-worn wireless sensors," *Sensors*, vol. 16, no. 5, p. 713, May 2016.
- [22] Ł. Januszkiwicz, P. D. Barba, and S. Hausman, "Automated identification of human-body model parameters," *Intel. Journal Appl. Electrom. Mechan.*, vol. 51, no. s1, pp. S41–S47, Apr 2016.
- [23] U. Singh, H. Kumar, and T. S. Kamal, "Design of yagi-uda antenna using biogeography based optimization," *IET Microw., Antennas Propag.*, vol. 58, no. 10, pp. 3375–3379, Oct 2010.

- [24] B. Liu, D. Zhao, P. Reynaert, and G. G. Gielen, "GASPAD: A general and efficient mm-wave integrated circuit synthesis method based on surrogate model assisted evolutionary algorithm," *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, vol. 33, no. 2, pp. 169–182, 2014.
- [25] M. Jamil and X.-S. Yang, "A literature survey of benchmark functions for global optimisation problems," *Intel. Journal Math. Modelling and Numerical Optim.*, vol. 4, no. 2, pp. 150–194, Feb 2013.
- [26] E. Mezura-Montes, J. Velázquez-Reyes, and C. A. Coello Coello, "A comparative study of differential evolution variants for global optimization," in *Proc. 8th Annu. Conf. Genetic Evol. Comput.* ACM, 2006, pp. 485–492.
- [27] S. Das and P. N. Suganthan, "Differential evolution: A survey of the state-of-the-art," *IEEE Trans. Evol. Comput.*, vol. 15, no. 1, pp. 4–31, Feb 2011.
- [28] Y. Wang, Z. Cai, and Q. Zhang, "Differential evolution with composite trial vector generation strategies and control parameters," *IEEE Trans. Evol. Comput.*, vol. 15, no. 1, pp. 55–66, Feb 2011.
- [29] J. Brest, S. Greiner, B. Boskovic, M. Mernik, and V. Zumer, "Self-adapting control parameters in differential evolution: A comparative study on numerical benchmark problems," *IEEE Trans. Evol. Comput.*, vol. 10, no. 6, pp. 646–657, Dec 2006.
- [30] R. Gämperle, S. D. Müller, and P. Koumoutsakos, "A parameter study for differential evolution," *Advances in Intelligent Systems, Fuzzy systems, Evolutionary Computation*, pp. 293–298, 2002.
- [31] J. Ronkkonen, S. Kukkonen, and K. V. Price, "Real-parameter optimization with differential evolution," in *Congr. Evol. Comput.*, vol. 1. IEEE, 2005, pp. 506–513.
- [32] A. K. Qin and P. N. Suganthan, "Differential evolution algorithm with strategy adaptation for global numerical optimization," *IEEE Trans. Evol. Comput.*, vol. 13, no. 2, pp. 1785–1791, Apr 2005.
- [33] J. Vesterstrom and R. Thomsen, "A comparative study of differential evolution, particle swarm optimization, and evolutionary algorithms on numerical benchmark problems," in *Congr. Evol. Comput.*, vol. 2. IEEE, 2004, pp. 1980–1987.
- [34] J. Kennedy and R. Eberhart, "Particle swarm optimization," in *Proc. Intel. Conf. Neural Networks*, vol. 4. IEEE, 1995, pp. 1942–1948.
- [35] R. C. Eberhart, Y. Shi, and J. Kennedy, *Swarm intelligence*. Elsevier, 2001.
- [36] W. Xia, X. Shang, and M. J. Lancaster, "Responses comparisons for coupled-resonator based diplexers," in *3rd Annu. Semi. Pass. RF Microw. Compon.* IET, 2012, pp. 67–75.



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